Content Review

Baumol-Tobin Model

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- Opportunity cost of holding money (as cash): foregone interest i.
- Cost of withdrawing money from deposits: K.
- B-T model answers the question as to how much and how often should funds be withdrawn to finance the purchase of Y given the associated costs.

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