

# Baumol-Tobin Model of Money Demand

- Individuals purchase  $Y$  over a fixed time interval with money. Money as cash or deposits.
- Opportunity cost of holding money (as cash) is  $i$ .
- Cost of withdrawing money (from deposits) is  $K$ .
- B-T model answers the question as to how much and how often should funds be withdrawn to finance the purchase of  $Y$  given the associated costs.

# Baumol-Tobin Model of Money Demand

- The goal is to minimize costs of financing the purchase. Suppose individual withdraws  $M$  units of money each time.
- If agent withdraws once, average money holding is given as  $(M + 0)/2 = M/2$ .
- Total costs = withdrawal cost + opportunity cost (of holding money)
- Withdrawal cost =  $K \cdot \frac{Y}{M}$ .
- Opportunity cost =  $i \cdot \frac{M}{2}$

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$$\text{Total cost} = K \cdot \frac{Y}{M} + i \cdot \frac{M}{2}.$$

We can minimise this by taking the derivative with respect to  $M$ :

$$-K \cdot \frac{Y}{M^2} + \frac{i}{2} = 0 \rightarrow M = \sqrt{\frac{2KY}{i}} \rightarrow \frac{M}{2} = \sqrt{\frac{KY}{2i}}$$

- Average holdings create the money demand

$$M^d = \sqrt{\frac{KY}{2i}}$$